Exercises 1 Sets

Intersection, complement, union, number sets

Objectives

- understand what a set, an element of a set, an intersection, a union, a complement is.
- know the set of real numbers, rational numbers, integers, natural numbers.
- be able to perform basic set operations.

Problems

1.1 Look at the sets A, B, and C:

A = Set of all the cities of the world

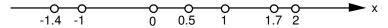
B = Set of all the European cities

C = Set of all the coastal cities of the world

Find at least four elements of the following sets:

- a) $B \cap C$
- b) B\C

- c) C \ B
- d) $A \setminus (B \cup C)$
- When calculating we usually deal with **real numbers**. The set \mathbb{R} of real numbers can be thought of as an infinitely long continuous number line. Each point of the number line represents a real number x:



The following number sets are subsets of \mathbb{R} :

 $\mathbb{N} = \text{Set of natural numbers} = \{1, 2, 3, 4, ...\}$

 \mathbb{Z} = Set of **integers** = {..., -4, -3, -2, -1, 0, 1, 2, 3, 4, ...}

 $\mathbb{Q} = \text{Set of } \mathbf{rational } \mathbf{numbers} = \left\{ x \mid x = \frac{m}{n}; \ m \in \mathbb{Z}; \ n \in \mathbb{Z}; \ n \in \mathbb{Z} \backslash \{0\} \right\}$

A rational number x is a number that can be expressed as a fraction $\frac{m}{n}$, where both numerator m and denominator n are integers and n is not zero.

- a) Determine the following sets:
 - i) **Z****N**
- ii) $\mathbb{Z} \cup \mathbb{N}$
- iii) $\mathbb{Z} \cap \mathbb{N}$
- b) Decide whether each statement is true or false:
 - i) $\mathbb{N} \subset \mathbb{Z}$
- ii) $\mathbb{Z} \subset \mathbb{Q}$
- iii) $\mathbb{Q} \subset \mathbb{R}$
- c) * Try to think of numbers that are elements of the set $\mathbb{R} \setminus \mathbb{Q}$
- 1.3 Harshbarger/Reynolds: Exercises 0.1, pages 6 to 9 (photocopies)

(Harshbarger, R.J. and Reynolds, J.J.: Mathematical Applications for the Management, Life, and Social Sciences, Houghton Mifflin Company, Boston / New York 2007, 8th edition, ISBN 978-0-618-73162-6)

Answers

- 1.1 a) $B \cap C = \{Lisbon, Copenhagen, Barcelona, Naples, Stockholm, ...\}$
 - b) B \ C = {London, Paris, Madrid, Berlin, Rome, ...}
 - c) C \ B = {Tokyo, San Francisco, Sydney, Rio de Janeiro, ...}
 - d) $A \setminus (B \cup C) = \{Chicago, Mexico City, Nairobi, Beijing, ...\}$
- 1.2 a) i) $\mathbb{Z} \setminus \mathbb{N} = \{0, -1, -2, -3, ...\}$
 - ii) $\mathbb{Z} \cup \mathbb{N} = \mathbb{Z}$
 - iii) $\mathbb{Z} \cap \mathbb{N} = \mathbb{N}$
 - b) i) true
 - ii) true
 - iii) true
 - c) * $\mathbb{R} \setminus \mathbb{Q} = \{\sqrt{2}, \sqrt{3}, \pi, ...\}$
- 1.3 see Harshbarger/Reynolds (photocopies)