

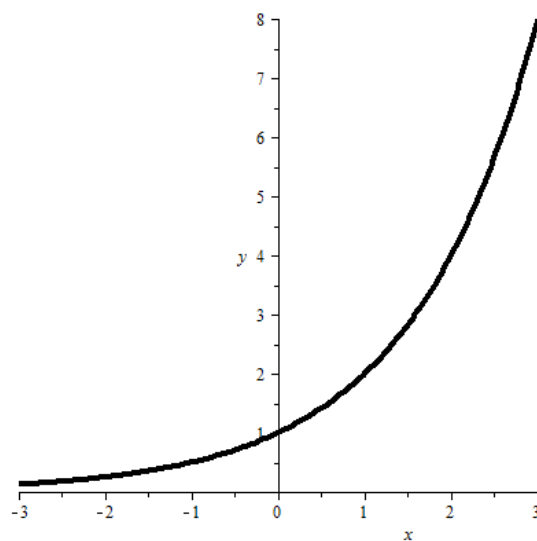
Exponentialfunktion

Definition

f:	$D \rightarrow \mathbb{R}$	$(D \subseteq \mathbb{R})$
$x \mapsto$	$y = f(x) = c \cdot a^x$	$(a \in \mathbb{R}^+ \setminus \{1\}, c \in \mathbb{R} \setminus \{0\})$
$a > 1$: exponentielles Wachstum		
$a < 1$: exponentieller Zerfall		

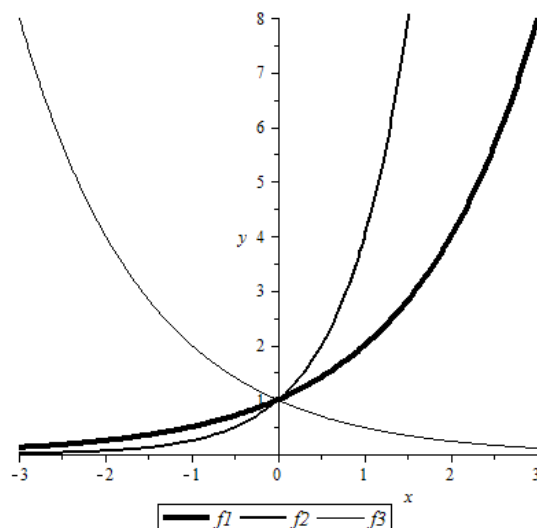
Graf

1. $y = f(x) = 2^x$ ($c = 1, a = 2$)



2. Parameter **a**

$$\begin{aligned} y &= f_1(x) = 2^x & (c = 1, a = 2) \\ y &= f_2(x) = 4^x & (c = 1, a = 4) \\ y &= f_3(x) = \left(\frac{1}{2}\right)^x & \left(c = 1, a = \frac{1}{2}\right) \end{aligned}$$

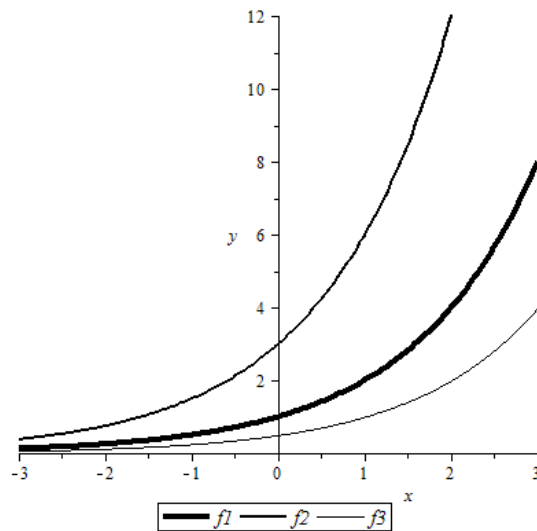


3. Parameter **c**

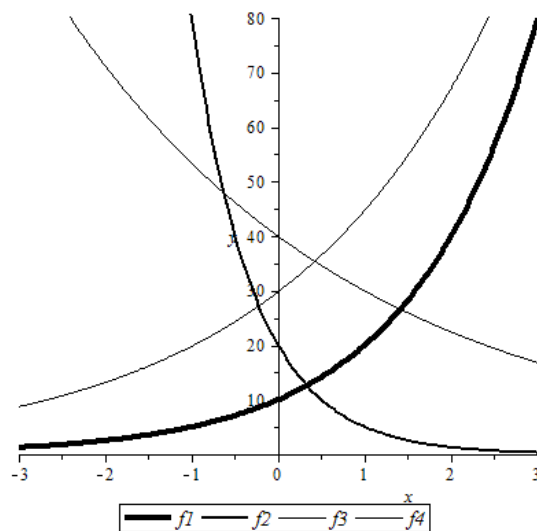
$$y = f_1(x) = 2^x \quad (c = 1, a = 2)$$

$$y = f_2(x) = 3 \cdot 2^x \quad (c = 3, a = 2)$$

$$y = f_3(x) = \frac{1}{2} \cdot 2^x \quad (c = \frac{1}{2}, a = 2)$$



4. $y = f_1(x) = 10 \cdot 2^x \quad (c = 10, a = 2)$
 $y = f_2(x) = 20 \cdot 0.25^x \quad (c = 20, a = 0.25)$
 $y = f_3(x) = 40 \cdot 0.75^x \quad (c = 40, a = 0.75)$
 $y = f_4(x) = 30 \cdot 1.5^x \quad (c = 30, a = 1.5)$



Beispiele

1. Zinseszins (exponentielles **Wachstum**)

$$K_n = K_0 \cdot q^n$$

K_0 = Anfangskapital

K_n = Kapital nach n Zinsperioden

n = Anzahl Zinsperioden (häufig: 1 Zinsperiode = 1 Jahr)

q = Zins-/Wachstumsfaktor = $1 + i$ ($q > 1$)

i = Zinssatz pro Zinsperiode

$$\text{Bsp.: } K_0 := 1000, i := 2\% = 0.02 \Rightarrow q = 1.02 \Rightarrow K_n = 1000 \cdot 1.02^n$$

2. Preisindex (exponentieller **Zerfall**)

$$P(t) = P_0 \cdot q^t$$

P_0 = Anfangspreis / anfängliche Kaufkraft

P(t) = Preis / Kaufkraft zum Zeitpunkt t (häufig: t in Jahren)

q = Zerfallsfaktor ($q < 1$)

$$\text{Bsp.: } P_0 := 100, q := 0.97 \Rightarrow P(t) = 100 \cdot 0.97^t$$