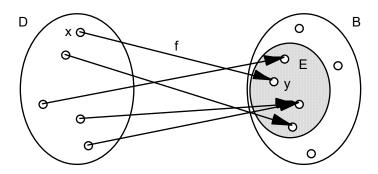
# **Function**

#### **Definition and examples**

Def.: A function f is a rule that associates to each element x in a set D exactly one element y in a set B.

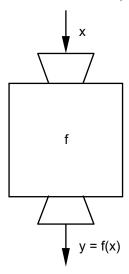


The function f **maps** the set D onto the set B.

f: 
$$D \rightarrow B$$
  
  $x \mapsto y = f(x)$  ("f of x")

The set D is the **domain**, the set B is the **codomain**, and the set E is the **range** of the function f.

The element y is the **image** of the element x. or (if D and B are number sets): y is the **value** of f at x.

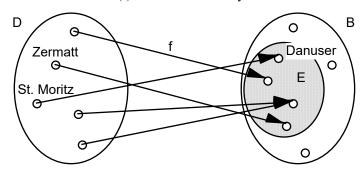


Ex.: 1. D = set of all Swiss holiday resorts

B = set of all human beings

 $f: D \rightarrow B$ 

 $r \mapsto d = f(r) = director of holiday resort r in 2000$ 



2. D = set of all countries of the world

B = set of all cities of the world

 $f: D \rightarrow B$ 

 $a \mapsto b = f(a) = capital of country a$ 

3. Cable car company

 $D = \mathbb{N}$  (= set of natural numbers)

 $B = \mathbb{R}$  (= set of real numbers)

f:  $D \rightarrow B$ 

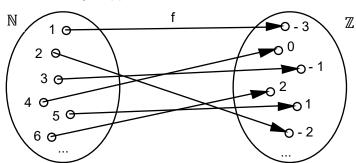
 $n \mapsto r = f(n) = \text{revenue (e.g. in CHF)}$  when n tickets are sold

4.  $D = \mathbb{N}$ 

$$\mathbf{B} = \mathbb{Z}$$

f:  $\mathbb{N} \to \mathbb{Z}$ 

$$n \mapsto y = f(n) = n - 4$$



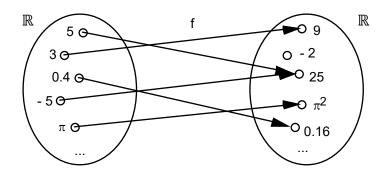
- 5.  $D = B = \mathbb{R}$ 
  - p:  $\mathbb{R} \to \mathbb{I}$

$$\mathbb{R} \to \mathbb{R}$$

$$x \mapsto y = p(x) = \frac{x^3 - 3}{2x^2 + 1}$$

## Representation of a function

#### Arrow diagram



#### Table of values

X	у
1	1
3	9
5	25
- 5	25
0.4	0.16

### Equation

#### Graph

